

**There have been a few changes to the syllabus for the October 2013 exam. I have posted a free supplement on my webpage [www.howardmahler.com/Teaching](http://www.howardmahler.com/Teaching) It covers all of the changes.**

I have included a discussion of each of the new topics, as well as problems to do. At the end of the supplement are a new Practice Exam and new Seminar Style Slides, covering the new material.

**page 63:** The probability generating functions of the zero-truncated distributions are given in Appendix B.

The probability generating functions of the zero-modified distributions are given in terms of those of the corresponding zero-truncated distribution, by:  $PM[z] = p_0^M + (1 - p_0^M) P^T[z]$ .

**page 398:** For  $\theta = 10$

**page 495 & 511:** If applying the Chi-Square Goodness of Fit Test to data with total claims and exposures by year, then the number of degrees of freedom is the number of years **minus the number of fitted parameters**.

Page 996:

In general,

the Bayes Estimate of the mean is:

$$\frac{\int (\text{Mean given } q) \pi(q) \text{ Prob}(\text{Obs.} | q) dq}{\int \pi(q) \text{ Prob}(\text{Obs.} | q) dq}$$

Page 998: **6.43. B.** If  $b$  were 300, then claim sizes are uniform from 300 to 400, and we could observe a claim of size 300.

If  $b$  were 200, then claim sizes are uniform from 200 to 300, and we could observe a claim of size 300.

$b$  can be 200, 300, or anything in between.

Given  $200 \leq b \leq 300$ , the chance of the observation given  $b$  is  $1/100$ .

$$\pi(b) = e^{-b/80} / 80.$$

The probability weight is:  $(e^{-b/80} / 80) (1/100)$ .

$\Rightarrow$  Posterior distribution of  $b$  is proportional to:

$$e^{-b/80}, 200 \leq b \leq 300.$$

$$\int_{200}^{300} e^{-b/80} db = -80 e^{-b/80} \Bigg|_{b=200}^{b=300}$$

$$= 80 (e^{-2.5} - e^{-3.75}) = 4.685.$$

Thus the posterior distribution of  $b$  is:

$$\frac{e^{-b/80}}{4.685}, 200 \leq b \leq 300.$$

Given  $b$ , the mean severity is:  $b + 50$ .

⇒ The expected value of the next claim from

the same insured is: 
$$\int_{200}^{300} (b + 50) \frac{e^{-b/80}}{4.685} db =$$

$$\frac{1}{4.685} \int_{200}^{300} b e^{-b/80} db + 50 \int_{200}^{300} \frac{e^{-b/80}}{4.685} db =$$

$$\frac{1}{4.685} \left( -80b e^{-b/80} - 80^2 e^{-b/80} \right) \Big|_{b=200}^{b=300} +$$

$$(50)(1) = 239.845 + 50 = \mathbf{289.845}.$$

Comment: The integral of the posterior density of  $b$  over its support has to be one.

See 4, 11/01, Q.14 (2009 Sample Q.64).