

In June 2022, the CAS announced that effective with the Fall 2022 exam sittings, the guessing penalty for exams MAS-I and MAS-II will be eliminated.

Therefore, you should make sure to choose a letter response for every question.

Read the portion of my second study guide on Bayes Analysis prior to the McElreath textbook.

1, page 6:

1 - Z is sometimes referred to as the “complement of credibility”.

Confusingly, often instead what I have denoted Y, the item that is given weight 1 - Z, is referred to as the “complement of credibility”.

Tse in Nonlife Actuarial Models: Theory Methods and Evaluation does not use the term “complement of credibility”. Weight 1 - Z is given to M = manual rate.

2, page 208, last line: = **0.4259**.

2, solution 6.3: $(24)(1/\omega)(1/\omega)(1/\omega)(1/\omega) = 24/\omega^4$. Final solution is okay.

2, page 306, 5th line from the bottom: $(300)^2(0.21)$

3, solution 5.1: $f(x) = \{(a+b-1)! / (a-1)! (b-1)!\} (x/\theta)^{a-1} \{1 - (x/\theta)\}^{b-1} / \theta =$

3, Q. 6.45: a Beta Distribution with $\theta = 1$

3, solution 7.46: $a' = a + \# \text{ successes} = 9 + 15 = 24$, and $b' = b + \# \text{ failures} = 5 + 25 = 30$. Posterior mean is: $a' / (a' + b') = 24 / (24 + 30) = \mathbf{0.444}$.

3, Q. 13.12: What is the posterior density function for the parameter θ for this insured?

3, Solution: 13.28: Thus at $x = 1, 8, 27, 125$, the densities are proportional to:

$\beta^{-1/3} \exp(-\beta^{-1/3})$, $\beta^{-1/3} \exp(-2 \beta^{-1/3})$, $\beta^{-1/3} \exp(-3 \beta^{-1/3})$, and $\beta^{-1/3} \exp(-5 \beta^{-1/3})$.

3, page 275, solutions 8.16 and 8.17 are missing:

8.16. E. A Gamma-Exponential with prior Gamma with $\alpha = 1$ and $\theta = 1/100$.

Thus the posterior Gamma has parameters $\alpha = 1 + 2 = 3$, and $1/\theta = 100 + 40 + 80 = 220$.

$E[1/\lambda]$ = negative first moment of the posterior Gamma = $220/(3-1) = \mathbf{110}$.

Alternately, the posterior distribution is proportional to: $e^{-100\lambda} \lambda e^{-40\lambda} \lambda e^{-80\lambda} = \lambda^2 e^{-220\lambda}$.

$E[X | \lambda] = 1/\lambda$. Therefore, the expected size of the next claim is:

$$\frac{\int_0^{\infty} (1/\lambda) \lambda^2 e^{-220\lambda} d\lambda}{\int_0^{\infty} \lambda^2 e^{-220\lambda} d\lambda} = \frac{220^2 \Gamma(2)}{220^3 \Gamma(3)} = 220/2 = \mathbf{110}.$$

Comment: Since $\alpha = 1 \leq 2$, one can not apply Buhlmann Credibility.

The posterior mixed distribution is Pareto with $\alpha = 3$ and $\theta = 220$, with mean $220/(3-1) = 110$.

8.17. D. A Gamma-Exponential.

Thus the posterior Gamma has parameters $\alpha = 4 + 3 = 7$,

and $1/\theta = 1000 + 100 + 200 + 500 = 1800$.

$E[1/\lambda]$ = negative first moment of the posterior Gamma = $1800/(7-1) = \mathbf{300}$.

Alternately, $K = \alpha - 1 = 4 - 1 = 3$. $Z = (3/(3+K)) = 3/(3+3) = 50\%$.

The prior mean is the negative first moment of the prior Gamma = $1000/(4-1) = 1000/3$.

Estimate of the future severity is: $(50\%)(800/3) + (50\%)(1000/3) = \mathbf{300}$.

Comment: The posterior mixed distribution is Pareto with $\alpha = 7$ and $\theta = 1800$, with mean $1800/(7-1) = 300$.

4, solution 4.39: $Z = 150/(150+0.986) = 0.9935$.

Estimated future pure premium is: $(0.9935)(3130.20) + (1 - 0.9935)(2783.49) = 3128$.

Estimated aggregate claim amount for the next period: $(3128)(175) = 547,400$.

5, Q. 2.10: Model III: K-Nearest Neighbors with $K = 5$.

5, page 88, third paragraph from the bottom:

Thus the **Gini Index** for a region is: $(2)(\text{proportion of yeses})(\text{proportion of nos})$.

5, Q.4.3: For observation 6, $\text{LoyalCH} = 0.695$.

(For given $\text{LoyalCH} = 0.795$, the prediction would be CH.)

5, solution. 8.16: Final solution is okay.

Z_1 and Z_3 are uncorrelated. It turns out that constraining Z_3 to be uncorrelated with Z_1 is equivalent to constraining the direction ϕ_3 to be orthogonal (perpendicular)

to the direction ϕ_1 . Thus, $\sum_{j=1}^5 \phi_{j1} \phi_{j3} = 0$. Thus Statement III is true.

Comment: Z_1 , Z_2 , and Z_3 are each orthogonal to the others.

5, Q. 10.13: $x_1 = (-1, 0)$ $x_3 = (2, -1)$,

5, Solution 10.1: {56} is 21 from {77}

Then on the second page of the solution.

{23, 39} is $\{(56 - 23) + (56 - 39) + (77 - 23) + (77 - 39)\}/4 = 35.5$ away from {56, 77}.

Final solution is okay.