

**Rewrite Exam 1, question 11:** One has fit a regression model with 6 variables (5 independent variables plus the intercept), to 18 observations.

One is testing the hypothesis  $H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = 0$ ,

versus the alternative hypothesis that  $H_0$  is false.

**TSS is the total sum of squares.**

**RSS is the residual (error) sum of squares.**

What is the critical region for a test at a 1% significance level?

- A.  $TSS \geq 3.1$  RSS
- B.  $TSS \geq 3.2$  RSS
- C.  $TSS \geq 3.3$  RSS
- D.  $TSS \geq 3.4$  RSS
- E.  $TSS \geq 3.5$  RSS

Solution to the revised question at the end of the errata.

**Exam 1, solution 9:**  $\text{Var}[\hat{\beta}_0] = 0.0431$ . Final answer is okay.

**Exam 2, question 18:** the  $r^{\text{th}}$  value from smallest to largest is:

**Exam 2, solution 38:** The final balance equation should be:  $0.1\pi_1 + 0.2\pi_2 + 0.5\pi_3 = \pi_3$ .

The final solution is okay.

**Exam 2, solution 42:**  $14S_1^2/\sigma_1^2$  is Chi-Square with 14 degrees of freedom.

**Exam 3, solution 1:** those with  $x$  values closest to  $x_0$  get more weight

**Exam 3, solution 15:**  $(y_t - y_{t-1}) = 0.3(y_{t-1} - y_{t-2}) - 0.5(y_{t-2} - y_{t-3}) + w_t + 0.4w_{t-1} + 0.2w_{t-2}$ .

Final answer is okay.

**Exam 4, solution 11:** The smoothed density at **70** is:

**Exam 4, solution 35:** The main limitation of GAMs is that the model is restricted to be additive. However, we can add interaction terms by including additional predictors such as  $X_j X_k$ .

In addition we could add low-dimensional interaction functions of the form  $f_{jk}(X_j, X_k)$  into the model.

Thus while "GAMs allow one to include interaction terms." is not a listed advantage of GAMs, the question would be much better without the given choice D.

I will change the question to:

- D. The smoothness of each function on a predictor can be summarized via degrees of freedom.
- E. All of the above are advantages of GAMs.

**Exam 6, Q. 24:** You are given a sample of size **four**: 11, 12, 12, 16.

**Exam 6, sol. 28-30:** In the table the total degrees of freedom should be **(3)(4)(2) = 24**

**Exam 6, sol. 37:** Final answer is okay.

The squared error is:  $\sum (y_i - \beta_0 - \beta_1 x_i - \beta_2 x_i^2)^2$ .

$$0 = \frac{\partial \text{squared error}}{\partial \beta_0} = \sum -2 (y_i - \beta_0 - \beta_1 x_i - \beta_2 x_i^2).$$

$$0 = \frac{\partial \text{squared error}}{\partial \beta_1} = \sum -2 x_i (y_i - \beta_0 - \beta_1 x_i - \beta_2 x_i^2).$$

$$0 = \frac{\partial \text{squared error}}{\partial \beta_2} = \sum -2 x_i^2 (y_i - \beta_0 - \beta_1 x_i - \beta_2 x_i^2).$$

**Exam 7, sol. 35,** in the Comment: if each component follows an **Exponential distribution**

**Exam 8, Q. 36**

A.  $x_t = w_t - 0.8w_{t-1} + 0.6w_{t-2}$  and  $y_t = 0.8y_{t-1} + w_t$

B.  $x_t = w_t - 0.8w_{t-1} + 0.6w_{t-2}$  and  $y_t = -0.8y_{t-1} + w_t$

C.  $x_t = w_t - 0.8w_{t-1} + 0.6w_{t-2} - 0.4w_{t-3}$  and  $y_t = 0.8y_{t-1} + w_t$

D.  $x_t = w_t - 0.8w_{t-1} + 0.6w_{t-2} - 0.4w_{t-3}$  and  $y_t = -0.8y_{t-1} + w_t$

**Exam 8, sol. 12,** next to last line:  $3p70$  Final solution is okay.

**Exam #9, sol. 7:**  $\theta = 1/\lambda = 1/(1/2) = 2$ .

**Exam #9, sol. 26:**  $1 + 5 + 4 + 3 + 2 + 1 = 16$  models. Statement III is false.

**Exam #12, sol. 21:** Applying this with  $k = -3$  and  $\tau = 3$ :  $E[1/X^3] = \theta^{-3} \Gamma[1 - (-3)/3]$

**Exam #13, sol. 24:**  $\text{Prob}[\text{category is } j \text{ or less}] = \frac{\exp[\beta_0j + \beta_1x_1 + \beta_2x_2 + \beta_3x_3]}{1 + \exp[\beta_0j + \beta_1x_1 + \beta_2x_2 + \beta_3x_3]}$ .

Final solution is okay.

**Solution to rewritten Exam 1, question 11:**

**11. A.** Compute F-Statistic =  $\frac{(TSS - RSS) / (k-1)}{RSS / (N - k)} = \frac{(TSS - RSS) / (6-1)}{RSS / (18 - 6)}$

= 2.4 (TSS - RSS) / RSS.

F has  $k - 1 = 5$ , and  $N - 5 = 12$  degrees of freedom, and the 1% critical value is 5.06.

Critical region is when we reject  $H_0$ , which is when  $F \geq 5.06$ .  $\Rightarrow$

$2.4 (TSS - RSS) / RSS \geq 5.06$ .  $\Rightarrow$  **TSS  $\geq$  3.11 RSS.**